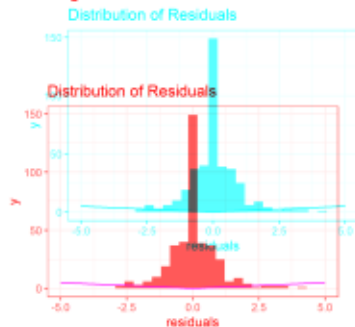


# Introduction to Machine Learning



## Advanced Risk Minimization vs. Maximum Likelihood Estimation vs. Empirical Risk Minimization



### Learning goals

- Correspondence between Laplace errors and L1 loss
- Correspondence between Bernoulli targets and the Bernoulli / log loss
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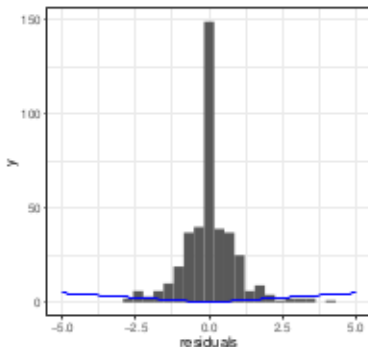


## LAPLACE ERRORS - L1-LOSS / 3

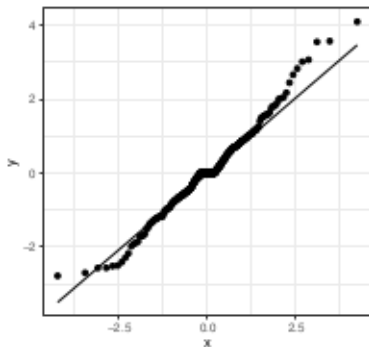
- We simulate data  $y | \mathbf{x} \sim \text{Laplacian}(f_{\text{true}}(\mathbf{x}), 1)$  with  $f_{\text{true}} = 0.2 \cdot \mathbf{x}$ .
- We can plot the empirical error distribution, i.e. the distribution of the residuals after fitting a regression model w.r.t.  $L_1$ -loss.
- With the help of a Q-Q-plot we can compare the empirical residuals vs. the theoretical quantiles of a Laplacian distribution.



Distribution of Residuals



Residuals vs. Quantiles of Error Distribution



## MAXIMUM LIKELIHOOD IN CLASSIFICATION / 2

This gives rise to the following loss function

$$L(y, \pi(\mathbf{x})) = -y \log(\pi(\mathbf{x})) - (1 - y) \log(1 - \pi(\mathbf{x})), \quad y \in \{0, 1\}$$

which we introduced as **Bernoulli** loss.

