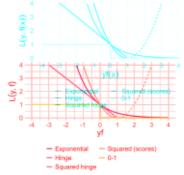
# Introduction to Machine Learning

# Advanced Risk Minimization ses

## Advanced Classification Losses



#### Learning goals

- Know the (squared) hinge loss
- Know the L2 loss defined on

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   Know the (squared) hinge loss
- Know the (Squared) hinge to
- Know the AUC loss
   Know the L2 loss defined on scores
- Know the exponential loss
- Know the AUC loss

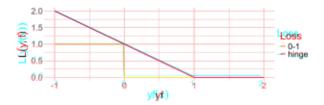


#### HINGE LOSS

- The intuitive appeal of the 0-1-loss is set off by its analytical properties ill-suited to direct optimization.
- The hinge loss is a continuous relaxation that acts as a convex upper bound on the 0-1-loss (for y ∈ {-1, +1}):

$$L(\mathbf{y},(\mathbf{y},\mathbf{y})) = \max\{0,1-yf\}\mathbf{x})\}.$$

- Note that the hinge loss only equals zero for a margin ≥ 1, encouraging confident (correct) predictions.
- It resembles a door hinge, hence the name:



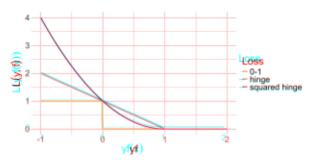


### SQUARED HINGE LOSS

• We can also specify a squared version for the hinge loss:

$$L(J_{(yx)}) = \max\{0, (1 - yf)\}^{2}\}$$

- The L2 form punishes margins yf (€)(0, 1) less severely but puts a high penalty on an ore confidently wrong predictions.
- Therefore, it is smoother yet more outlier-sensitive than the non-squared hinge loss.





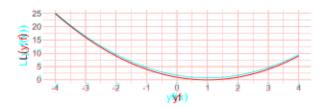
#### SQUARED LOSS ON SCORES

 Analogous to the Brier score defined on probabilities we can specify a squared loss on classification scores (again, y ∈ {-1, +1}, using that y² ≡ 1):

$$L(y, f(x)(y+f) \Leftrightarrow -(y(x))f)^{2} = yy^{2} - 22yfx + f^{2}(x))^{2} =$$

$$= -12yf2yf + (yf)x^{2}) + (1yf)^{2}yf(x)^{2}$$

 This loss behaves just like the squared hinge loss for yf (x)1, but is zerosonly for yf for 1/a(nd) actually lincreases agains for larger for margins (which (is line general not idesirable!) rable!)





### CLASSIFICATION LOSSES: EXPONENTIAL LOSS

Another possible choice for a (binary) loss function that is a smooth approximation to the 0-1-loss is the **exponential loss**:

- L(y, f) ⇒ exp(xpyf), used in AdaBoost Boost.
- Convex, differentiable (thus easier to optimize than 0-1-loss).
- The loss increases exponentially for wrong predictions with high confidence; if the prediction is right with a small confidence only, there, loss is still positive.
- No closed-form analytic solution to (empirical) risk minimization.

