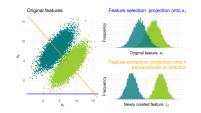
# Introduction to Machine Learning

Feature Selection **Feature Selection: Introduction** 





#### Learning goals

- Too many features can be harmful in prediction
- Selection vs. extraction
- Types of selection methods

### INTRODUCTION

Feature selection:

Finding a well-performing, hopefully small set of features for a task.

Feature selection is critical for

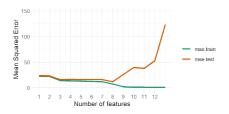
- reducing noise and overfitting
- improving performance/generalization
- enhancing interpretability by identifying most informative features

Features can be selected based on domain knowledge, or data-driven algorithmic approaches. We focus on the latter here.



### **MOTIVATION**

- Naive view:
  - ullet More features o more information o discriminant power  $\uparrow$
  - Model is not harmed by irrelevant features since their parameters can simply be estimated as 0.
- In practice, irrelevant and redundant features can "confuse" learners (see **curse of dimensionality**) and worsen performance.
- Example: In linear regression,  $R^2$  is monotonically increasing in p, but adding irrelevant features leads to overfitting (capturing noise).





### **MOTIVATION /2**

- In high-dimensional data sets, we often have prior information that many features are either irrelevant or of low quality
- Having redundant features can cost something during prediction (money or time)
- Many models require n > p data. Thus, we either need to
  - adapt models to high-dimensional data (e.g., regularization)
  - design entirely new procedures for p > n data
  - use filter preprocessing methods from this lecture



### **SIZE OF DATASETS**

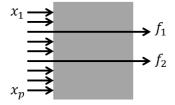
Many new forms of technical measurements and connected data leads to availability of extremely high-dimensional data sets.

- Classical setting: Up to around 10<sup>2</sup> features, feature selection might be relevant, but benefits often negligible.
- Datasets of medium to high dimensionality: At around 10<sup>2</sup> to 10<sup>3</sup> features, classical approaches can still work well, while principled feature selection helps in many cases.
- **High-dimensional data**:  $10^3$  to  $10^9$  or more features. Examples: micro-array / gene expression data and text categorization (bag-of-words features). If we also have few observations, scenario is called  $p \gg n$ .



# FEATURE SELECTION VS. EXTRACTION

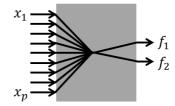
#### Feature selection



- Creates a subset of original features x by selecting p

  features f.
- Retains information on selected individual features.

#### **Feature extraction**



- Maps p features in x to p
   extracted features f.
- Info on individual features can be lost through (non-)linear combination.



# FEATURE SELECTION VS. EXTRACTION /2

- Both FS and FE contribute to
   1) dimensionality reduction and 2) simplicity of models
- FE can be unsupervised (PCA, multidim scaling, manifold learning) or supervised (supervised PCA, partial least squares)
- FE can produce lower dim projections which can work better than FS; whether FE+model is interpretable depends on how interpretable extracted features are







## TYPES OF FEATURE SELECTION METHODS

In rest of the chapter, we introduce different types of methods for FS:

- Filters: evaluate relevance of features using statistical properties such as correlation with target variable
- Wrappers: use a model to evaluate subsets of features
- Embedded methods: integrate FS directly into specific model we look at them in their dedicated chapters (e.g., CART, L<sub>0</sub>, L<sub>1</sub>)

**Example: embedded method (Lasso)** regularizing model params with *L*1 penalty enables "automatic" feature selection:

$$\mathcal{R}_{\text{reg}}(oldsymbol{ heta}) = \mathcal{R}_{\text{emp}}(oldsymbol{ heta}) + \lambda \|oldsymbol{ heta}\|_1 = \sum_{i=1}^n \left( y^{(i)} - oldsymbol{ heta}^ op \mathbf{x}^{(i)} 
ight)^2 + \lambda \sum_{j=1}^p | heta_j|$$

