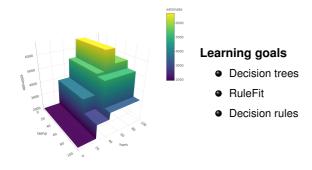
# **Interpretable Machine Learning**

# **Rule-based Models**





### DECISION TREES > Breiman et al. (1984)

Idea of decision trees: Partition data into subsets based on cut-off values in features (found by minimizing a split criterion via greedy search) and predict constant mean  $c_m$ in leaf node  $\mathcal{R}_m$ :

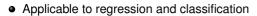
$$\hat{f}(x) = \sum_{m=1}^{M} c_m \mathbb{1}_{\{x \in \mathcal{R}_m\}}$$

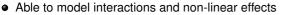


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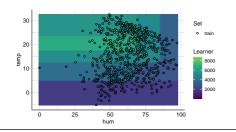
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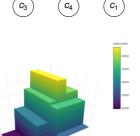
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 Able to handle mixed feature spaces and missing values







 $x_1 \ge 3$ 

### INTERPRETATION

- Directly by following the tree structure (i.e., sequence of decision rules)
- Importance of  $x_j$ : Aggregate "improvement in split criterion" over all splits where  $x_j$  was involved

 $\rightsquigarrow$  e.g., variance for regression or Gini index for classification

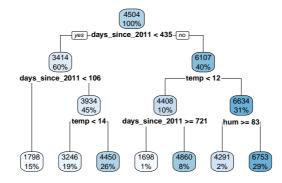


### **DECISION TREES - EXAMPLE**

- Fit decision tree with tree depth of 3 on bike data
- E.g., mean prediction for the first 105 days since 2011 is 1798
   → Applies to =15% of the data (leftmost branch)
- days\_since\_2011: highest feature importance (explains most of variance)



Feature	Importance
days_since_2011	79.53
temp	17.55
hum	2.92



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- Selection bias towards high-cardinal/continuous features
- Does not consider significant improvements when splitting (→ overfitting)



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- Separate selection of feature used for splitting and split point
- A Hypothesis test as stopping criteria



► Hothorn et al. (2006) ➤ Zeileis et al. (2008) ➤ Strobl et al. (2007)

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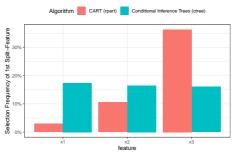
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#### Example (selection bias):

Simulate data (n = 200) with  $Y \sim N(0, 1)$ and 3 features of different cardinality independent from *Y* (repeat 500 times):

- $X_1 \sim Binom(n, \frac{1}{2})$
- $X_2 \sim M(n, (\frac{1}{4}, \frac{1}{4}, \frac{1}{4}, \frac{1}{4}))$
- $X_3 \sim M(n, (\frac{1}{8}, \frac{1}{8}, \frac{1}{8}, \frac{1}{8}, \frac{1}{8}, \frac{1}{8}, \frac{1}{8}, \frac{1}{8}))$

Which feature is selected in the first split?





#### Differences to CART:

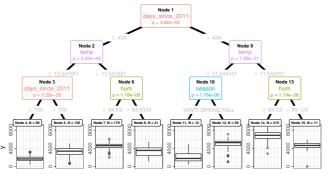
- Two-step approach (1. find most significant split feature, 2. find best split point)
- Parametric model (e.g. LM instead of constant) can be fitted in leave nodes
- Significance of split (p-value) given in each node
- ctree and mob differ in hypothesis test used for selecting the split feature (independence test vs. fluctuation test) and how to find the best split point



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**Example** (ctree): Bike data (constant model in final nodes)



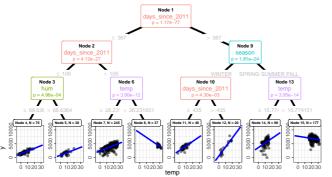
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**Example** (mob): Bike data (linear model with temp in final nodes)



Train error (MSE): 758,844.0 (ctree) 742,244.4 (mob)



## **OTHER RULE-BASED MODELS**

#### Decision Rules > Holte 1993

- ◆ (Chaining of) simple "if then" statements
   → very intuitive and easy-to-interpret
- Most methods work only for classification and categorical features

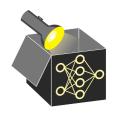
IF size=small THEN value=low
IF size=medium THEN value=medium
IF size=big THEN value=high



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  IF size=medium THEN value=medium
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#### RuleFit Friedman and Popescu 2008

- Combination of LM and decision trees
- Uses (many) decision trees to extract important decision rules r<sub>1</sub>, r<sub>2</sub>, r<sub>3</sub>, r<sub>4</sub> which are used as features in a (regularized) LM
- Allows for feature interactions and non-linearities

