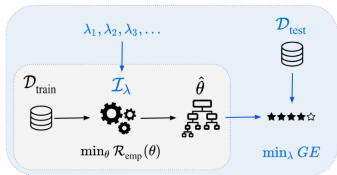


# Hyperparameter Tuning Introduction

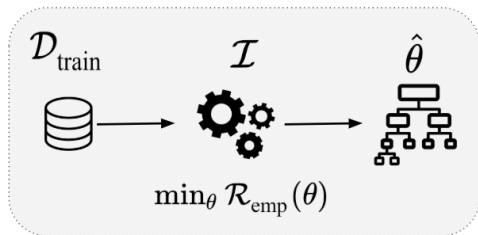


- Understand the difference between model parameters and hyperparameters
- Know different types of hyperparameters
- Be able to explain the goal of hyperparameter tuning



# MOTIVATING EXAMPLE

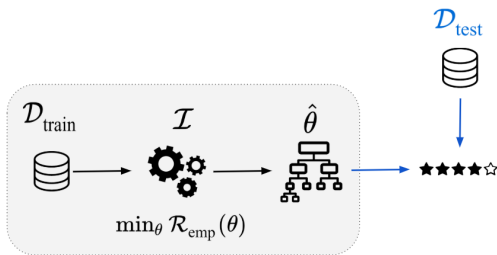
- Given a data set, we want to train a classification tree.
- We feel that a maximum tree depth of 4 has worked out well for us previously, so we decide to set this hyperparameter to 4.
- The learner ("inducer")  $\mathcal{I}$  takes the input data, internally performs **empirical risk minimization**, and returns a fitted tree model  $\hat{f}(\mathbf{x}) = f(\mathbf{x}, \hat{\theta})$  of at most depth  $\lambda = 4$  that minimizes empirical risk.



## MOTIVATING EXAMPLE / 2

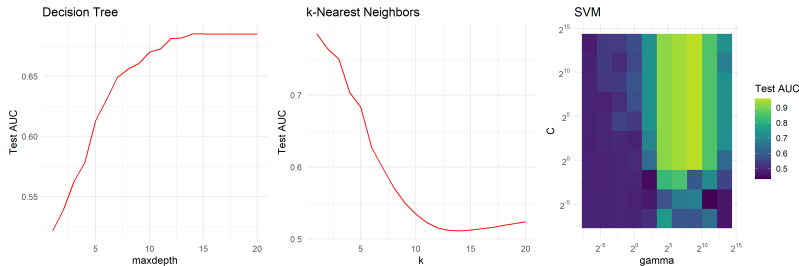
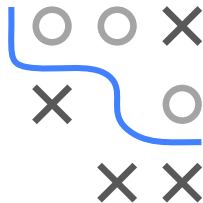
- We are **actually** interested in the **generalization performance**  $\text{GE}(\hat{f})$  of the estimated model on new, previously unseen data.
- We estimate the generalization performance by evaluating the model  $\hat{f} = \mathcal{I}(\mathcal{D}_{\text{train}}, \lambda)$  on a test set  $\mathcal{D}_{\text{test}}$ :

$$\widehat{\text{GE}}_{\mathcal{D}_{\text{train}}, \mathcal{D}_{\text{test}}}(\mathcal{I}, \lambda, n_{\text{train}}, \rho) = \rho(\mathbf{y}_{\mathcal{D}_{\text{test}}}, \mathbf{F}_{\mathcal{D}_{\text{test}}, \hat{f}})$$



## MOTIVATING EXAMPLE / 3

- But many ML algorithms are sensitive w.r.t. a good setting of their hyperparameters, and generalization performance might be bad if we have chosen a suboptimal configuration.
- Consider a simulation example of 3 ML algorithms below, where we use the dataset *mlbench.spiral* and 10,000 testing points. As can be seen, varying hyperparameters can lead to big difference in model's generalization performance.





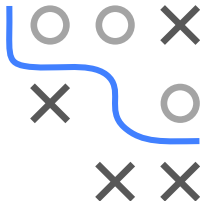
# MODEL PARAMETERS VS. HYPERPARAMETERS

It is critical to understand the difference between model parameters and hyperparameters.

**Model parameters**  $\theta$  are optimized during training. They are an **output** of the training.

Examples:

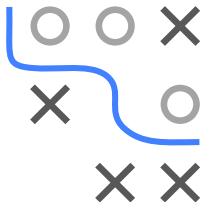
- The splits and terminal node constants of a tree learner
- Coefficients  $\theta$  of a linear model  $f(\mathbf{x}) = \theta^\top \mathbf{x}$



# MODEL PARAMETERS VS. HYPERPARAMETERS

/ 2

In contrast, **hyperparameters** (HPs)  $\lambda$  are not optimized during training. They must be specified in advance, are an **input** of the training. Hyperparameters often control the complexity of a model, i.e., how flexible the model is. They can in principle influence any structural property of a model or computational part of the training process.



The process of finding the best hyperparameters is called **tuning**.

Examples:

- Maximum depth of a tree
- $k$  and which distance measure to use for  $k$ -NN
- Number and maximal order of interactions to be included in a linear regression model
- Number of optimization steps if the empirical risk minimization is done via gradient descent

# TYPES OF HYPERPARAMETERS

We summarize all hyperparameters we want to tune in a vector  $\lambda \in \Lambda$  of (possibly) mixed type. HPs can have different types:

- Real-valued parameters, e.g.:
  - Minimal error improvement in a tree to accept a split
  - Bandwidths of the kernel density estimates for Naive Bayes
- Integer parameters, e.g.:
  - Neighborhood size  $k$  for  $k$ -NN
  - $mtry$  in a random forest
- Categorical parameters, e.g.:
  - Which split criterion for classification trees?
  - Which distance measure for  $k$ -NN?

Hyperparameters are often **hierarchically dependent** on each other, e.g., *if* we use a kernel-density estimate for Naive Bayes, what is its width?

