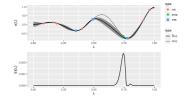
## **Introduction to Machine Learning**

# Hyperparameter Tuning Advanced Tuning Techniques



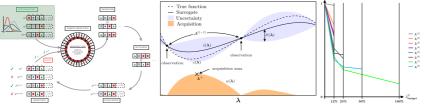


#### Learning goals

- Basic idea of evolutionary algorithms
- and Bayesian Optimization
- and hyperband

#### **HPO - MANY APPROACHES**

- Evolutionary algorithms
- Bayesian / model-based optimization
- Multi-fidelity optimization, e.g. Hyperband



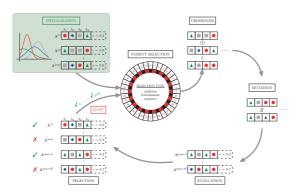
HPO methods can be characterized by:

- how the exploration vs. exploitation trade-off is handled
- how the inference vs. search trade-off is handled

Further aspects: Parallelizability, local vs. global behavior, handling of noisy observations, multifidelity and search space complexity.



#### **EVOLUTIONARY STRATEGIES**



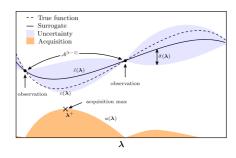


- Are a class of stochastic population-based optimization methods inspired by the concepts of biological evolution
- Are applicable to HPO since they do not require gradients
- Mutation is the (randomized) change of one or a few HP values in a configuration.
- Crossover creates a new HPC by (randomly) mixing the values of two other configurations.

BO sequentially iterates:

- Approximate  $\lambda \mapsto c(\lambda)$  by (nonlin) regression model  $\hat{c}(\lambda)$ , from evaluated configurations (archive)
- **Propose candidates** via optimizing an acquisition function that is based on the surrogate  $\hat{c}(\lambda)$
- **Sevaluate** candidate(s) proposed in 2, then go to 1

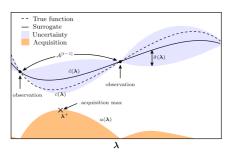
Important trade-off: **Exploration** (evaluate candidates in under-explored areas) vs. **exploitation** (search near promising areas)





#### Surrogate Model:

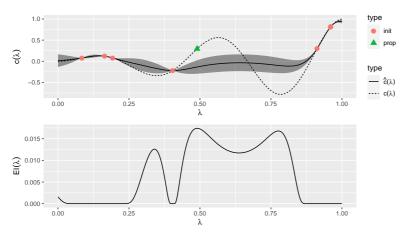
- Probabilistic modeling of  $C(\lambda) \sim (\hat{c}(\lambda), \hat{\sigma}(\lambda))$  with posterior mean  $\hat{c}(\lambda)$  and uncertainty  $\hat{\sigma}(\lambda)$ .
- Typical choices for numeric spaces are Gaussian Processes; random forests for mixed spaces





#### **Acquisition Function:**

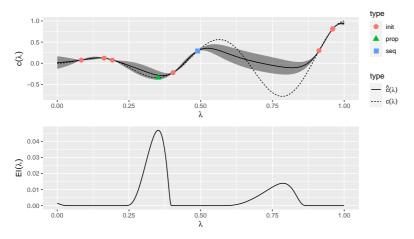
- Balance exploration (high  $\hat{\sigma}$ ) vs. exploitation (low  $\hat{c}$ ).
- Lower confidence bound (LCB):  $a(\lambda) = \hat{c}(\lambda) \kappa \cdot \hat{\sigma}(\lambda)$
- Expected improvement (EI):  $a(\lambda) = \mathbb{E} \left[ \max \left\{ c_{\min} C(\lambda), 0 \right\} \right]$  where  $(c_{\min}$  is best cost value from archive)
- Optimizing  $a(\lambda)$  is still difficult, but cheap(er)





Upper plot: The surrogate model (black, solid) models the *unknown* relationship between input and output (black, dashed) based on the initial design (red points).

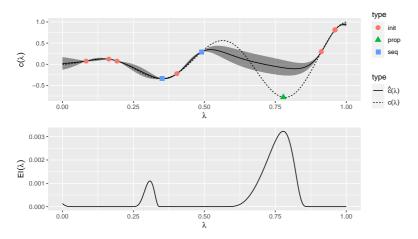
Lower plot: Mean and variance of the surrogate model are used to derive the expected improvement (EI) criterion. The point that maximizes the EI is proposed (green point).





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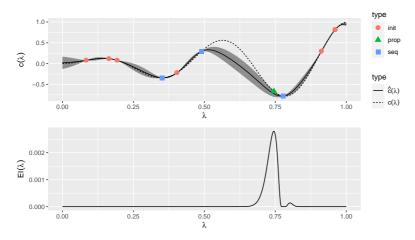
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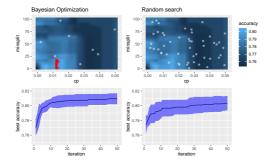
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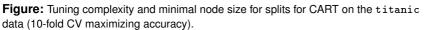




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Since we use the sequentially updated surrogate model predictions of performance to propose new configurations, we are guided to "interesting" regions of  $\Lambda$  and avoid irrelevant evaluations:





Left panel: BO, 50 configurations; right panel: random search, 50 iterations.

Top panel: one run (initial design of BO is white); bottom panel: mean  $\pm$  std of 10 runs.





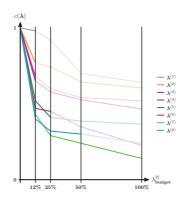
#### **MULTIFIDELITY OPTIMIZATION**

- Prerequiste: Fidelity HP  $\lambda_{\rm fid}$ , i.e., a component of  $\lambda$ , which influences the computational cost of the fitting procedure in a monotonically increasing manner
- Methods of multifidelity optimization in HPO are all tuning approaches that can efficiently handle a  $\mathcal{I}$  with a HP  $\lambda_{\text{fid}}$
- The lower we set  $\lambda_{\rm fid}$ , the more points we can explore in our search space, albeit with much less reliable information w.r.t. their true performance.
- We assume to know box-constraints of  $\lambda_{\text{fid}}$ , so  $\lambda_{\text{fid}} \in [\lambda_{\text{fid}}^{\text{low}}, \lambda_{\text{fid}}^{\text{upp}}]$ , where the upper limit implies the highest fidelity returning values closest to the true objective value at the highest computational cost.



#### **SUCCESSIVE HALVING**

- Races down set of HPCs to the best
- Idea: Discard bad configurations early
- Train HPCs with fraction of full budget (SGD epochs, training set size); the control param for this is called multi-fidelity HP
- Continue with better  $1/\eta$  fraction of HPCs (w.r.t  $\widehat{\rm GE}$ ); with  $\eta$  times budget (usually  $\eta=2,3$ )
- Repeat until budget depleted or single HPC remains





#### **MULTIFIDELITY OPTIMIZATION – HYPERBAND**

#### **Problem with SH**

 Good HPCs could be killed off too early, depends on evaluation schedule

#### Solution: Hyperband

- Repeat SH with different start budgets  $\lambda_{\text{fid}}^{[0]}$  and initial number of HPCs  $p^{[0]}$
- Each SH run is called bracket
- Each bracket consumes ca. the same budget

or	$\eta$	=	4	
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bracket 3			
i		$\lambda_{fid}^{[t]}$	$p_3^{[t]}$
(	)	1	82
-	1 4	4	20
2	2	16	5
3	3 (	64	1

	bracket 2		
	t	$\lambda_{fid}^{[t]}$	$p_2^{[t]}$
-	0	4	27
	1	16	6
	2	64	1

	bracke	t 1
t	$\lambda_{fid}^{[t]}$	$p_1^{\iota_1}$
0	16	10
4	61	2

	bracket	t 0
t	$\lambda_{fid}^{[t]}$	$p_0^{[t]}$
0	64	5



#### **MORE TUNING ALGORITHMS:**

Other advanced techniques besides model-based optimization and the hyperband algorithm are:

- Stochastic local search, e.g., simulated annealing
- Genetic algorithms / CMAES
- Iterated F-Racing
- Many more . . .

For more information see *Hyperparameter Optimization: Foundations, Algorithms, Best Practices and Open Challenges*, Bischl (2021)

