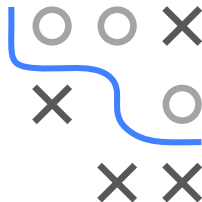


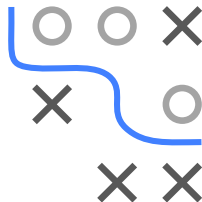
MOTIVATION

- The graphical way of representing simple functions/models, like logistic regression. Why is that useful?
- Because individual neurons can be used as building blocks of more complicated functions.
- Networks of neurons can represent extremely complex hypothesis spaces.
- Most importantly, it allows us to define the “right” kinds of hypothesis spaces to learn functions that are more common in our universe in a data-efficient way (see Lin, Tegmark et al. 2016).



REPRESENTATION LEARNING

- It is *very* critical to feed a classifier the “right” features in order for it to perform well.
- Before deep learning took off, features for tasks like machine vision and speech recognition were “hand-designed” by domain experts. This step of the machine learning pipeline is called **feature engineering**.
- DL automates feature engineering. This is called **representation learning**.



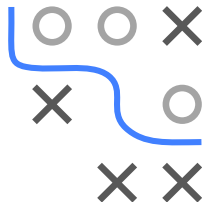
SINGLE HIDDEN LAYER NETWORKS

Single neurons perform a 2-step computation:

- ➊ **Affine Transformation:** a weighted sum of inputs plus bias.
- ➋ **Activation:** a non-linear transformation on the weighted sum.

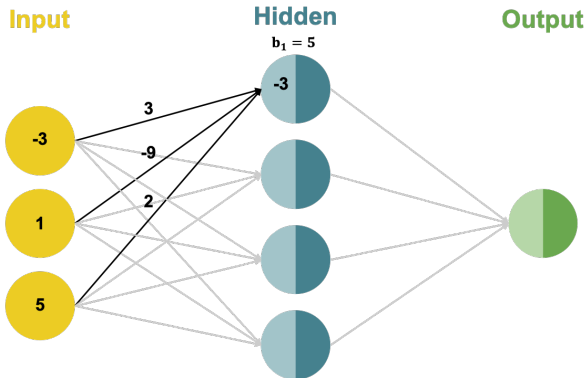
Single hidden layer networks consist of two layers (without input layer):

- ➊ **Hidden Layer:** having a set of neurons.
 - ➋ **Output Layer:** having one or more output neurons.
- Multiple inputs are simultaneously fed to the network.
 - Each neuron in the hidden layer performs a 2-step computation.
 - The final output of the network is then calculated by another 2-step computation performed by the neuron in the output layer.



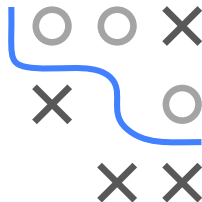
SINGLE HIDDEN LAYER NETWORKS: EXAMPLE

Each neuron in the hidden layer performs an **affine transformation** on the inputs:



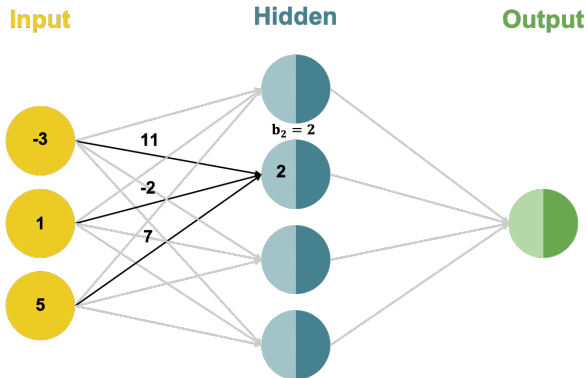
$$z_{in}^{(1)} = w_{11}x^{(1)} + w_{21}x^{(2)} + w_{31}x^{(3)} + b_1$$

$$z_{in}^{(1)} = 3 * (-3) + (-9) * 1 + 2 * 5 + 5 = -3$$



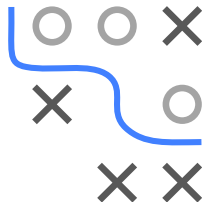
SINGLE HIDDEN LAYER NETWORKS: EXAMPLE

Each neuron in the hidden layer performs an **affine transformation** on the inputs:



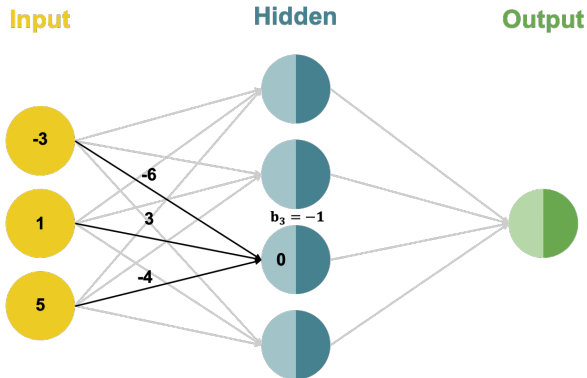
$$z_{in}^{(2)} = w_{12}x^{(1)} + w_{22}x^{(2)} + w_{32}x^{(3)} + b_2$$

$$z_{in}^{(2)} = 11 * (-3) + (-2) * 1 + 7 * 5 + 2 = 2$$

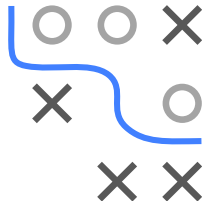


SINGLE HIDDEN LAYER NETWORKS: EXAMPLE

Each neuron in the hidden layer performs an **affine transformation** on the inputs:

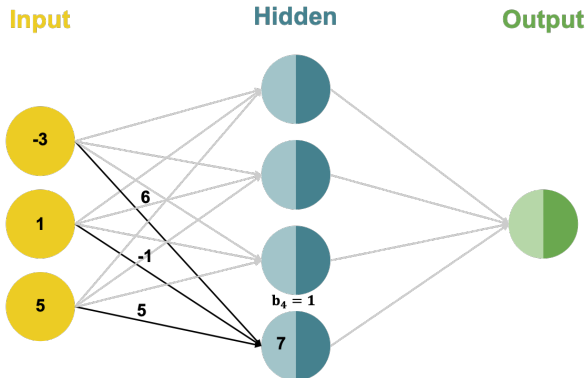


$$z_{in}^{(3)} = (-6) * (-3) + 3 * 1 + (-4) * 5 - 1 = 0$$

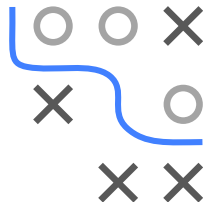


SINGLE HIDDEN LAYER NETWORKS: EXAMPLE

Each neuron in the hidden layer performs an **affine transformation** on the inputs:

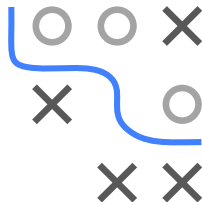
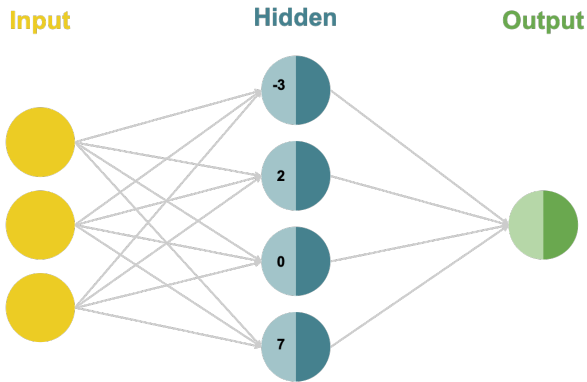


$$z_{in}^{(4)} = w_{14}x^{(1)} + w_{24}x^{(2)} + w_{34}x^{(3)} + b_4$$
$$z_{in}^{(4)} = 6 * (-3) + (-1) * 1 + 5 * 5 + 1 = 7$$



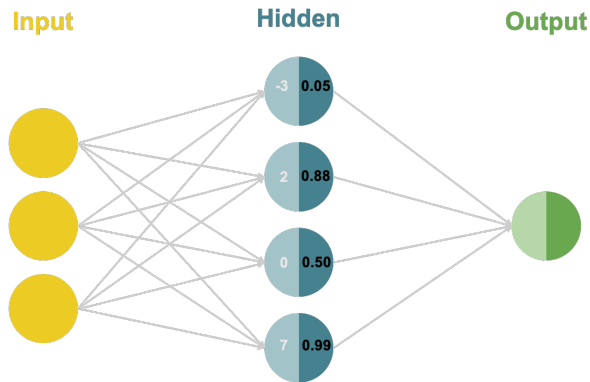
SINGLE HIDDEN LAYER NETWORKS: EXAMPLE

Each neuron in the hidden layer performs an **affine transformation** on the inputs:

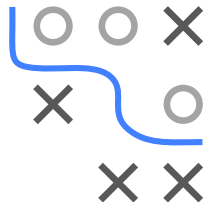


SINGLE HIDDEN LAYER NETWORKS: EXAMPLE

Each hidden neuron performs a non-linear **activation** transformation on the weight sum:

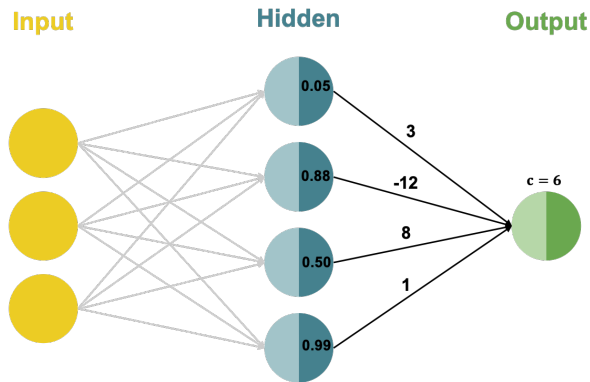


$$z_{\text{out}}^{(i)} = \sigma \left(z_{\text{in}}^{(i)} \right) = \frac{1}{1 + e^{-z_{\text{in}}^{(i)}}}$$

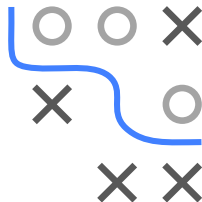


SINGLE HIDDEN LAYER NETWORKS: EXAMPLE

The output neuron performs an **affine transformation** on its inputs:

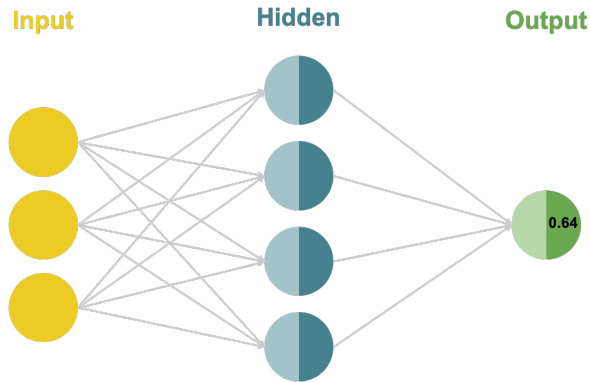


$$f_{\text{in}} = u_1 z_{\text{out}}^{(1)} + u_2 z_{\text{out}}^{(2)} + u_3 z_{\text{out}}^{(3)} + u_4 z_{\text{out}}^{(4)} + c$$

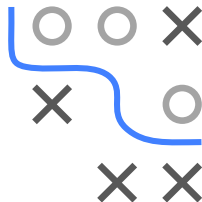


SINGLE HIDDEN LAYER NETWORKS: EXAMPLE

The output neuron performs a non-linear **activation** transformation on the weight sum:

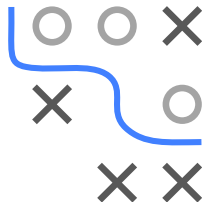


$$f_{\text{out}} = \sigma(f_{\text{in}}) = \frac{1}{1 + e^{f_{\text{in}}}}$$
$$f_{\text{out}} = \frac{1}{1 + e^{0.57}} = 0.64$$



HIDDEN LAYER: ACTIVATION FUNCTION

- If the hidden layer does not have a non-linear activation, the network can only learn linear decision boundaries.
- A lot of different activation functions exist.



HIDDEN LAYER: ACTIVATION FUNCTION

ReLU Activation:

- Currently the most popular choice is the ReLU (rectified linear unit):

$$\sigma(v) = \max(0, v)$$

