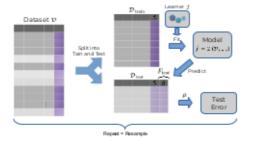
RESAMPLING

- Goal: estimate GE(I, λ, n, ρ_L) = E[L(y, I(D_{train}, λ)(x))].
- Holdout: Small trainset = high pessimistic bias; small testset = high var.
- Resampling: Repeatedly split in train and test, then average results.
- Allows to have large trainsets large (low pessimistic bias) since we use GE(I, λ, n_{train}, ρ) as a proxy for GE(I, λ, n, ρ))
- And reduce var from small testsets via averaging over repetitions.





RESAMPLING STRATEGIES

- Represent train and test sets by index vectors::
 J_{train} ∈ {1,...,n}^{n_{train}} and J_{test} ∈ {1,...,n}^{n_{test}}
- Resampling strategy = collection of splits:

$$\mathcal{J} = ((J_{\text{train},1}, J_{\text{test},1}), \dots, (J_{\text{train},B}, J_{\text{test},B})).$$

Resampling estimator:

$$\begin{split} \widehat{\mathrm{GE}}(\mathcal{I}, \mathcal{J}, \rho, \lambda) &= \mathrm{agr}\Big(\rho\Big(\mathbf{y}_{J_{\mathrm{test}, 1}}, \mathbf{\textit{F}}_{J_{\mathrm{test}, 1}, \mathcal{I}(\mathcal{D}_{\mathrm{train}, 1}, \lambda)}\Big), \\ &\vdots \\ &\rho\Big(\mathbf{y}_{J_{\mathrm{test}, B}}, \mathbf{\textit{F}}_{J_{\mathrm{test}, B}, \mathcal{I}(\mathcal{D}_{\mathrm{train}, B}, \lambda)}\Big)\Big), \end{split}$$

Aggregation agr is typically "mean" and n_{train} ≈ n_{train,1} ≈ · · · ≈ n_{train,B}.



CROSS-VALIDATION

- 5 or 10 folds are common.
- k = n is known as "leave-one-out" CV (LOO-CV)
- Bias of GE: The more folds, the smaller. LOO nearly unbiased.
- LOO has high var, better many folds for small data but not LOO
- Repeated CV (avg over high-fold CVs) good for for small data.



LEAVE-ONE-OBJECT-OUT

- Used when we have multiple obs from same objects, e.g., persons or hospitals or base images
- Data not i.i.d. any more
- Data from same object should either be in train or testset
- Otherwise we likely bias GE
- CV on objects, or leave-one-object-out

